

APPENDIX 7.3

CALCULATION OF THE CONTRIBUTION OF H₂S OXIDATION TO THE OXIDATION OF CuS.

An estimate of the possible contribution of this mechanism of oxidation to the total bacterial metabolism can be calculated from the following information;

a. The thermodynamic data of Wagman et al. (1968 & 1969) together with the data of Barton (1973) allows calculation of the maximum [H₂S] compatible with given pH and [Cu²⁺].

$$\text{Eq. 7.3.1} \quad \log[\text{H}_2\text{S}] = -15.6 - 2\text{pH} - \log[\text{Cu}^{2+}] \text{ at } 25^\circ\text{C}.$$

(concentrations in mol l⁻¹)

b. McLaren and Packer (1970) review the encounter rate theory of Smoluchowski which allows calculation of the maximum rate of H₂S uptake at the above concentration.

$$\text{Eq. 7.3.2} \quad \text{Encounter rate} = 4\pi R D[\text{H}_2\text{S}] \text{ molecules/sec}$$

where R = radius of a cell, (cm),

D = Fick's self diffusion coefficient for H₂S

(cm²/sec), and [H₂S] is in molecules per ml.

Data from Perry and Chilton (1973), suggests

$$D(\text{H}_2\text{S}) = 1.2 \times 10^{-5} \text{cm}^2/\text{sec}.$$

c. Page 3 of Meynell and Meynell (1970) states that 10⁹ Gram negative bacteria contain 300 µg dry weight. If 1/3 of this is carbon, then each cell requires 5 X 10⁹ carbon atoms to reproduce itself. In Appendix 7.2 it is shown that for every 12 carbon atoms fixed, at least 100 sulphur atoms are oxidized. Since each sulphur atom is

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equal to six reducing equivalents the number of reducing equivalents required by each cell to reduce a CO₂ molecule is $\frac{6 \times 100}{12} = 50$.

Therefore, to reproduce itself, each cell must oxidize 2.5×10^{11} reducing equivalents, or 3×10^{10} molecules of H₂S. (There are 8 reducing equivalents per H₂S molecule.)

At pH 2.5 and 10^{-4} M Cu²⁺,

$$\log[\text{H}_2\text{S}] = -15.6 - 5.0 + 4 = -16.6 \quad (\text{See Eq. 7.3.1}).$$

$$\text{i.e., } [\text{H}_2\text{S}] = 2.5 \times 10^{-17} \text{ mol l}^{-1} = 1.5 \times 10^4 \text{ molecules/ml}$$

Assuming $R = 10^{-4}$ cm

$$\begin{aligned} \text{Encounter rate} &= 4\pi \times 1.2 \times 10^{-5} \times 10^{-4} \times 1.5 \times 10^4 \\ &\qquad\qquad\qquad \text{molecules sec}^{-1} \\ &= 2 \times 10^{-4} \text{ molecules sec}^{-1} \end{aligned}$$

Therefore the time required for each cell to double using CuS generated H₂S as the sole substrate would be at least

$$\frac{3 \times 10^{10}}{2 \times 10^{-4}} \text{ sec.} \quad = 5 \text{ million years.}$$

Obviously this mechanism makes no contribution to CuS oxidation although it may be important for other sulphides.

APPENDIX 7.4CALCULATION OF THE CONTRIBUTION OF Cu⁺ TO
BACTERIAL OXIDATION OF CuS.

The method of calculation is the same as used in Appendix 7.3 and the sources of data are the same. The maximum [Cu⁺] compatible with CuS, S and a given [Cu²⁺] is;

$$\text{Eq.7.4.1} \quad \log[\text{Cu}^+] = -7.5 + \frac{1}{2}\log[\text{Cu}^{2+}] \quad (\text{concentrations in mol l}^{-1}) \text{ at } 25^\circ\text{C}$$

A method of estimating the self diffusion coefficients of ions is given in Perry and Chilton (1973). In this case there is no nett movement of anions but only a countercurrent movement of Cu⁺ and Cu²⁺. (The diffusion of H⁺ into the cell, necessary for stoichiometry, should not be rate limiting, given the high mobility of H⁺ in water). For the purposes of the calculation Cu²⁺ is treated as the anion accompanying Cu⁺. The result is;

$$D(\text{Cu}^+, \text{Cu}^{2+}) = 1.1 \times 10^{-5} \text{ cm}^2 \text{ sec}^{-1}.$$

To reproduce itself, each cell must oxidize at least 2.5×10^{11} Cu⁺ ions.

At 10^{-4}M Cu²⁺, $\log[\text{Cu}^+] = -7.5 - 2 = -9.5$ (See Eq. 7.4.1).

$$\text{i.e., } [\text{Cu}^+] = 3 \times 10^{-10} \text{ mol l}^{-1} = 2 \times 10^{11} \text{ molecules/ml}$$

$$\begin{aligned} \text{Encounter rate} &= 4\pi \times 10^{-4} \times 1.1 \times 10^{-5} \times 2 \times 10^{11} \text{ molecules sec}^{-1} \\ &= 3 \times 10^3 \text{ molecules sec}^{-1}. \end{aligned}$$

Therefore the time required for each cell to double using

$$\text{Cu}^+ \text{ produced by CuS would be at least } \frac{2.5 \times 10^{11}}{3 \times 10^3} \text{ sec}$$

$$= 3 \text{ years.}$$

This mechanism, therefore, makes no contribution to CuS oxidation. However, if a complex were present which

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stabilized Cu^+ , such that its concentration rose to $3 \times 10^{-7} \text{ mol l}^{-1}$, then the cyclic oxidation and reduction of cuprous and cupric ions could lead to a doubling time of one day, which is about the observed doubling time.